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# GW170104: Observation of a 50-Solar-Mass Binary Black Hole Coalescence at Redshift 0.2

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We describe the observation of GW170104, a gravitational-wave signal produced by the coalescence of a pair of stellar-mass black holes. The signal was measured on January 4, 2017 at 10:11:58.6 UTC by the twin advanced detectors of the Laser Interferometer Gravitational-Wave Observatory during their second observing run, with a network signal-to-noise ratio of 13 and a false alarm rate less than 1 in 70 000 years. The inferred component black hole masses are  $31.2^{+8.4}_{-6.0} M_{\odot}$  and  $19.4^{+5.3}_{-5.9} M_{\odot}$  (at the 90% credible level). The black hole spins are best constrained through measurement of the effective inspiral spin parameter, a mass-weighted combination of the spin components perpendicular to the orbital plane,  $\chi_{\text{eff}} = -0.12^{+0.21}_{-0.30}$ . This result implies that spin configurations with both component spins positively aligned with the orbital angular momentum are disfavored. The source luminosity distance is  $880^{+450}_{-390}$  Mpc corresponding to a redshift of  $z = 0.18^{+0.08}_{-0.07}$ . We constrain the magnitude of modifications to the gravitational-wave dispersion relation and perform null tests of general relativity. Assuming that gravitons are dispersed in vacuum like massive particles, we bound the graviton mass to  $m_g \leq 7.7 \times 10^{-23}$  eV/ $c^2$ . In all cases, we find that GW170104 is consistent with general relativity.

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## I. INTRODUCTION

The first observing run of the Advanced Laser Interferometer Gravitational-Wave Observatory (LIGO) [1] identified two binary black hole coalescence signals with high statistical significance, GW150914 [2] and GW151226 [3], as well as a less significant candidate LVT151012 [4,5]. These discoveries ushered in a new era of observational astronomy, allowing us to investigate the astrophysics of binary black holes and test general relativity (GR) in ways that were previously inaccessible [6,7]. We now know that there is a population of binary black holes with component masses  $\gtrsim 25 M_{\odot}$  [5,6], and that merger rates are high enough for us to expect more detections [5,8].

Advanced LIGO's second observing run began on November 30, 2016. On January 4, 2017, a gravitational-wave signal was detected with high statistical significance. Figure 1 shows a time-frequency representation of the data from the LIGO Hanford and Livingston detectors, with the signal GW170104 visible as the characteristic chirp of a binary coalescence. Detailed analyses demonstrate that GW170104 arrived at Hanford  $\sim 3$  ms before Livingston, and originated from the coalescence of two stellar-mass black holes at a luminosity distance of  $\sim 3 \times 10^9$  light-years.

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GW170104's source is a heavy binary black hole system, with a total mass of  $\sim 50 M_{\odot}$ , suggesting formation in a subsolar metallicity environment [6]. Measurements of the black hole spins show a preference away from being (positively) aligned with the orbital angular momentum, but do not exclude zero spins. This is distinct from the case for GW151226, which had a strong preference for spins with positive projections along the orbital angular momentum [3]. The inferred merger rate agrees with previous calculations [5,8], and could potentially be explained by binary black holes forming through isolated binary evolution or dynamical interactions in dense stellar clusters [6].

Gravitational-wave observations of binary black holes are the ideal means to test GR and its alternatives. They provide insight into regimes of strong-field gravity where velocities are relativistic and the spacetime is dynamic. The tests performed with the sources detected in the first observing run showed no evidence of departure from GR's predictions [5,7]; GW170104 provides an opportunity to tighten these constraints. In addition to repeating tests performed in the first observing run, we also test for modifications to the gravitational-wave dispersion relation. Combining measurements from GW170104 with our previous results, we obtain new gravitational-wave constraints on potential deviations from GR.

## II. DETECTORS AND DATA QUALITY

The LIGO detectors measure gravitational-wave strain using two dual-recycled Fabry-Perot Michelson interferometers at the Hanford and Livingston observatories [1,10].

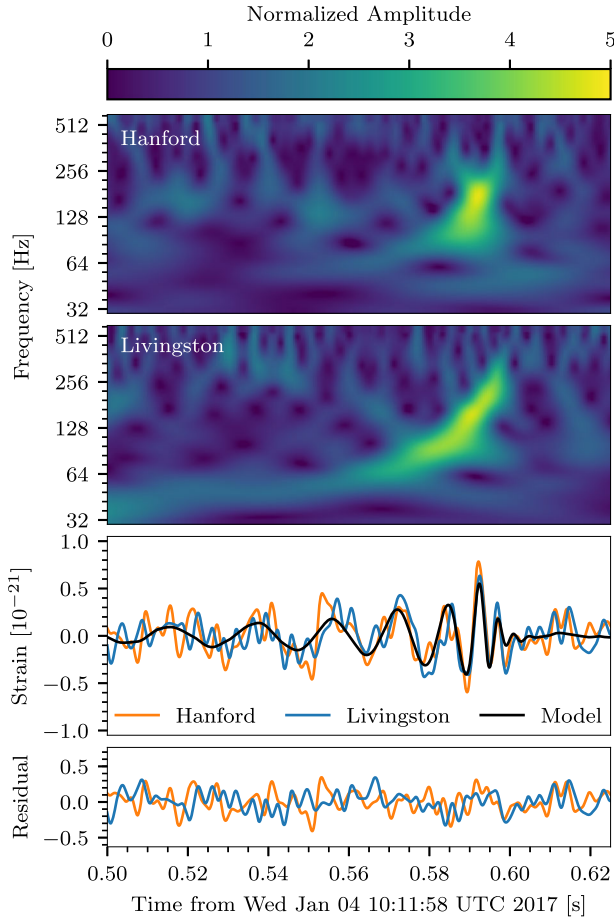


FIG. 1. Time–frequency representation [9] of strain data from Hanford and Livingston detectors (top two panels) at the time of GW170104. The data begin at 1167559936.5 GPS time. The third panel from the top shows the time-series data from each detector with a 30–350 Hz bandpass filter, and band-reject filters to suppress strong instrumental spectral lines. The Livingston data have been shifted back by 3 ms to account for the source’s sky location, and the sign of its amplitude has been inverted to account for the detectors’ different orientations. The maximum-likelihood binary black hole waveform given by the full-precession model (see Sec. IV) is shown in black. The bottom panel shows the residuals between each data stream and the maximum-likelihood waveform.

After the first observing run, both LIGO detectors underwent commissioning to reduce instrumental noise, and to improve duty factor and data quality (see Sec. I in the Supplemental Material [11]). For the Hanford detector, a high-power laser stage was introduced, and as the first step the laser power was increased from 22 to 30 W to reduce shot noise [10] at high frequencies. For the Livingston detector, the laser power was unchanged, but there was a significant improvement in low-frequency performance mainly due to the mitigation of scattered light noise.

Calibration of the interferometers is performed by inducing test-mass motion using photon pressure from modulated calibration lasers [12,13]. The one-sigma

calibration uncertainties for strain data in both detectors for the times used in this analysis are better than 5% in amplitude and  $3^\circ$  in phase over the frequency range 20–1024 Hz.

At the time of GW170104, both LIGO detectors were operating with sensitivity typical of the observing run to date and were in an observation-ready state. Investigations similar to the detection validation procedures for previous events [2,14] found no evidence that instrumental or environmental disturbances contributed to GW170104.

### III. SEARCHES

GW170104 was first identified by inspection of low-latency triggers from Livingston data [15–17]. An automated notification was not generated as the Hanford detector’s calibration state was temporarily set incorrectly in the low-latency system. After it was manually determined that the calibration of both detectors was in a nominal state, an alert with an initial source localization [18,19] was distributed to collaborating astronomers [20] for the purpose of searching for a transient counterpart. About 30 groups of observers covered the parts of the sky localization using ground- and space-based instruments, spanning from  $\gamma$  ray to radio frequencies as well as high-energy neutrinos [21].

Offline analyses are used to determine the significance of candidate events. They benefit from improved calibration and refined data quality information that is unavailable to low-latency analyses [5,14]. The second observing run is divided into periods of two-detector cumulative coincident observing time with  $\gtrsim 5$  days of data to measure the false alarm rate of the search at the level where detections can be confidently claimed. Two independently designed matched filter analyses [16,22] used 5.5 days of coincident data collected from January 4, 2017 to January 22, 2017.

These analyses search for binary coalescences over a range of possible masses and by using discrete banks [23–28] of waveform templates modeling binaries with component spins aligned or antialigned with the orbital angular momentum [29]. The searches can target binary black hole mergers with detector-frame total masses  $2M_\odot \leq M^{\text{det}} \lesssim 100\text{--}500M_\odot$ , and spin magnitudes up to  $\sim 0.99$ . The upper mass boundary of the bank is determined by imposing a lower limit on the duration of the template in the detectors’ sensitive frequency band [30]. Candidate events must be found in both detectors by the same template within 15 ms [4]. This 15-ms window is determined by the 10-ms intersite propagation time plus an allowance for the uncertainty in identified signal arrival times of weak signals. Candidate events are assigned a detection statistic value ranking their relative likelihood of being a gravitational-wave signal: the search uses an improved detection statistic compared to the first observing run [31]. The significance of a candidate event is calculated by comparing its detection statistic value to an estimate of the background noise [4,16,17,22]. GW170104 was detected

with a network matched-filter signal-to-noise ratio (SNR) of 13. At the detection statistic value assigned to GW170104, the false alarm rate is less than 1 in 70 000 years of coincident observing time.

The probability of astrophysical origin  $P_{\text{astro}}$  for a candidate event is found by comparing the candidate's detection statistic to a model described by the distributions and rates of both background and signal events [8,32,33]. The background distribution is analysis dependent, being derived from the background samples used to calculate the false alarm rate. The signal distribution can depend on the mass distribution of the source systems; however, we find that different models of the binary black hole mass distribution (as described in Sec. VI) lead to negligible differences in the resulting value of  $P_{\text{astro}}$ . At the detection statistic value of GW170104, the background rate in both matched filter analyses is dwarfed by the signal rate, yielding  $P_{\text{astro}} > 1 - (3 \times 10^{-5})$ .

An independent analysis that is not based on matched filtering, but instead looks for generic gravitational-wave bursts [2,34] and selects events where the signal frequency rises over time [35], also identified GW170104. This approach allows for signal deviations from the waveform models used for matched filtering at the cost of a lower significance for signals that are represented by the considered templates. This analysis reports a false alarm rate of  $\sim 1$  in 20 000 years for GW170104.

#### IV. SOURCE PROPERTIES

The source parameters are inferred from a coherent Bayesian analysis of the data from both detectors [36,37]. As a cross-check, we use two independent model-waveform families. Both are tuned to numerical-relativity simulations of binary black holes with nonprecessing spins, and introduce precession effects through approximate prescriptions. One model includes inspiral spin precession using a single effective spin parameter  $\chi_p$  [38–40]; the other includes the generic two-spin inspiral precession dynamics [41–43]. We refer to these as the effective-precession and full-precession models, respectively [44]. The two models yield consistent results. Table I shows selected source parameters for GW170104; unless otherwise noted, we quote the median and symmetric 90% credible interval for inferred quantities. The final mass (or equivalently the energy radiated), final spin, and peak luminosity are computed using averages of fits to numerical-relativity results [45–49]. The parameter uncertainties include statistical and systematic errors from averaging posterior probability distributions over the two waveform models, as well as calibration uncertainty [37] (and systematic uncertainty in the fit for peak luminosity). Statistical uncertainty dominates the overall uncertainty as a consequence of the moderate SNR.

For binary coalescences, the gravitational-wave frequency evolution is primarily determined by the component masses. For higher mass binaries, merger and ringdown dominate the

TABLE I. Source properties for GW170104: median values with 90% credible intervals. We quote source-frame masses; to convert to the detector frame, multiply by  $(1+z)$  [50,51]. The redshift assumes a flat cosmology with Hubble parameter  $H_0 = 67.9 \text{ km s}^{-1} \text{ Mpc}^{-1}$  and matter density parameter  $\Omega_m = 0.3065$  [52]. More source properties are given in Table I of the Supplemental Material [11].

Primary black hole mass $m_1$	$31.2^{+8.4}_{-6.0} M_\odot$
Secondary black hole mass $m_2$	$19.4^{+5.3}_{-5.9} M_\odot$
Chirp mass $\mathcal{M}$	$21.1^{+2.4}_{-2.7} M_\odot$
Total mass $M$	$50.7^{+5.9}_{-5.0} M_\odot$
Final black hole mass $M_f$	$48.7^{+5.7}_{-4.6} M_\odot$
Radiated energy $E_{\text{rad}}$	$2.0^{+0.6}_{-0.7} M_\odot c^2$
Peak luminosity $\ell_{\text{peak}}$	$3.1^{+0.7}_{-1.3} \times 10^{56} \text{ erg s}^{-1}$
Effective inspiral spin parameter $\chi_{\text{eff}}$	$-0.12^{+0.21}_{-0.30}$
Final black hole spin $a_f$	$0.64^{+0.09}_{-0.20}$
Luminosity distance $D_L$	$880^{+450}_{-390} \text{ Mpc}$
Source redshift $z$	$0.18^{+0.08}_{-0.07}$

signal, allowing good measurements of the total mass  $M = m_1 + m_2$  [53–57]. For lower mass binaries, like GW151226 [3], the inspiral is more important, providing precision measurements of the chirp mass  $\mathcal{M} = (m_1 m_2)^{3/5} / M^{1/5}$  [58–61]. The transition between the regimes depends upon the detectors' sensitivity, and GW170104 sits between the

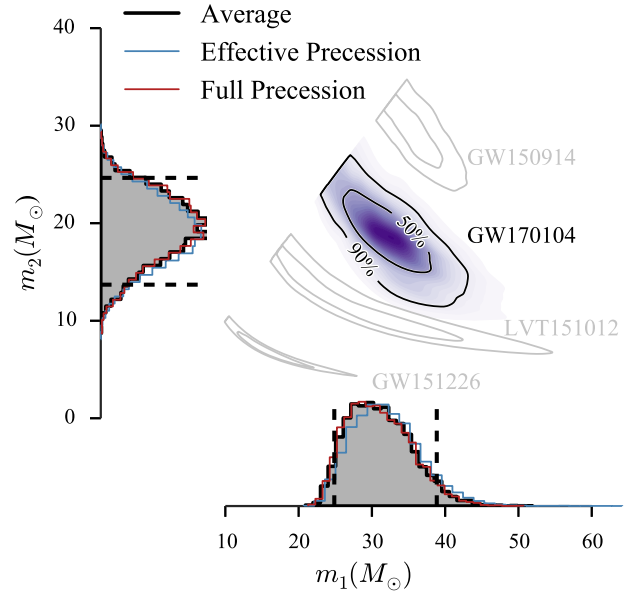


FIG. 2. Posterior probability density for the source-frame masses  $m_1$  and  $m_2$  (with  $m_1 \geq m_2$ ). The one-dimensional distributions include the posteriors for the two waveform models, and their average (black). The dashed lines mark the 90% credible interval for the average posterior. The two-dimensional plot shows the contours of the 50% and 90% credible regions plotted over a color-coded posterior density function. For comparison, we also show the two-dimensional contours for the previous events [5].



two. The inferred component masses are shown in Fig. 2. The form of the two-dimensional distribution is guided by the combination of constraints on  $M$  and  $\mathcal{M}$ . The binary was composed of two black holes with masses  $m_1 = 31.2^{+8.4}_{-6.0} M_\odot$  and  $m_2 = 19.4^{+5.3}_{-5.9} M_\odot$ ; these merged into a final black hole of mass  $48.7^{+5.7}_{-4.6} M_\odot$ . This binary ranks second, behind GW150914's source [5,37], as the most massive stellar-mass binary black hole system observed to date.

The black hole spins play a subdominant role in the orbital evolution of the binary, and are more difficult to determine. The orientations of the spins evolve due to precession [62,63], and we report results at a point in the inspiral corresponding to a gravitational-wave frequency of 20 Hz [37]. The effective inspiral spin parameter  $\chi_{\text{eff}} = (m_1 a_1 \cos \theta_{LS_1} + m_2 a_2 \cos \theta_{LS_2})/M$  is the most important spin combination for setting the properties of the inspiral [64–66] and remains important through to merger [67–71]; it is approximately constant throughout the orbital evolution [72,73]. Here  $\theta_{LS_i} = \cos^{-1}(\hat{\mathbf{L}} \cdot \hat{\mathbf{S}}_i)$  is the tilt angle between the spin  $\mathbf{S}_i$  and the orbital angular momentum  $\mathbf{L}$ , which ranges from  $0^\circ$  (spin aligned with orbital angular momentum) to  $180^\circ$  (spin antialigned);  $a_i = |c\mathbf{S}_i/Gm_i^2|$  is the (dimensionless) spin magnitude, which ranges from 0 to 1, and  $i = 1$  for the primary black hole and  $i = 2$  for the secondary. We use the Newtonian angular momentum for  $\mathbf{L}$ , such that it is normal to the orbital plane; the total orbital angular momentum differs from this because of post-Newtonian corrections. We infer that  $\chi_{\text{eff}} = -0.12^{+0.21}_{-0.30}$ . Similarly to GW150914 [5,37,44],  $\chi_{\text{eff}}$  is close to zero with a preference towards being negative: the probability that  $\chi_{\text{eff}} < 0$  is 0.82. Our measurements therefore disfavor a large total spin positively aligned with the orbital angular momentum, but do not exclude zero spins.

The in-plane components of the spin control the amount of precession of the orbit [62]. This may be quantified by the effective precession spin parameter  $\chi_p$  which ranges from 0 (no precession) to 1 (maximal precession) [39]. Figure 3 (top) shows the posterior probability density for  $\chi_{\text{eff}}$  and  $\chi_p$  [39]. We gain some information on  $\chi_{\text{eff}}$ , excluding large positive values, but, as for previous events [3,5,37], the  $\chi_p$  posterior is dominated by the prior (see Sec. III of the Supplemental Material [11]). No meaningful constraints can be placed on the magnitudes of the in-plane spin components and hence precession.

The inferred component spin magnitudes and orientations are shown in Fig. 3 (bottom). The lack of constraints on the in-plane spin components means that we learn almost nothing about the spin magnitudes. The secondary's spin is less well constrained as the less massive component has a smaller impact on the signal. The probability that the tilt  $\theta_{LS_i}$  is less than  $45^\circ$  is 0.04 for the primary black hole and 0.08 for the secondary, whereas the prior probability is 0.15 for each. Considering the two spins together, the probability that both tilt angles are less than  $90^\circ$  is 0.05.

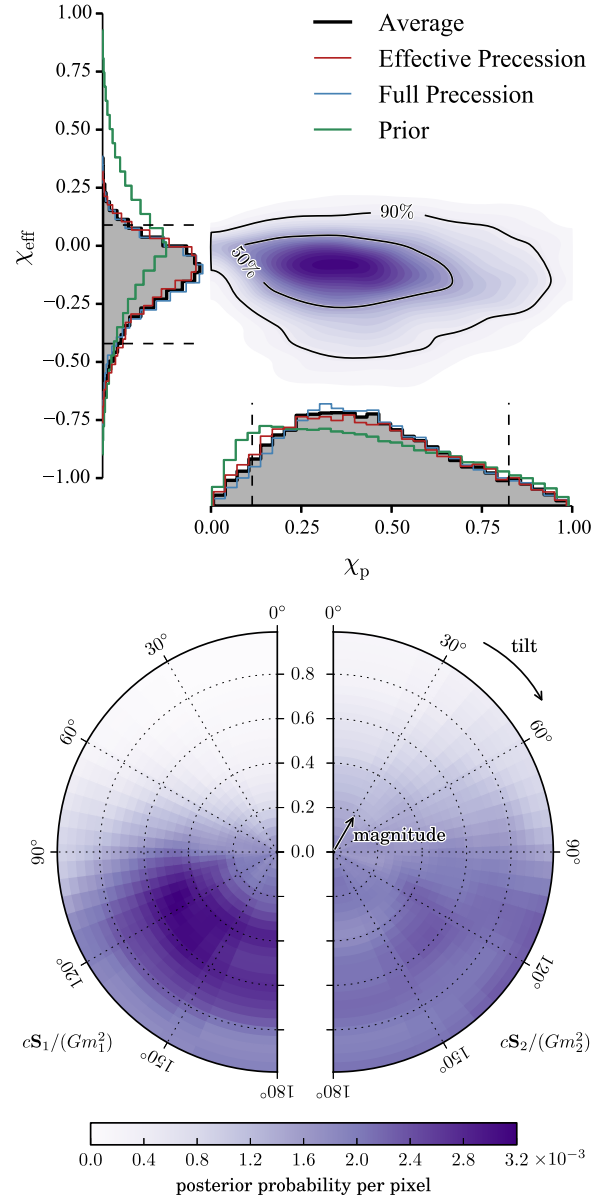


FIG. 3. *Top*: Posterior probability density for the effective inspiral and precession spin parameters,  $\chi_{\text{eff}}$  and  $\chi_p$ . The one-dimensional distributions show the posteriors for the two waveform models, their average (black), and the prior distributions (green). The dashed lines mark the 90% credible interval for the average posterior. The two-dimensional plot shows the 50% and 90% credible regions plotted over the posterior density function. *Bottom*: Posterior probabilities for the dimensionless component spins,  $c\mathbf{S}_1/(Gm_1^2)$  and  $c\mathbf{S}_2/(Gm_2^2)$ , relative to the normal of the orbital plane  $\hat{\mathbf{L}}$ . The tilt angles are  $0^\circ$  for spins aligned with the orbital angular momentum and  $180^\circ$  for spins antialigned. The probabilities are marginalized over the azimuthal angles. The pixels have equal prior probability ( $1.6 \times 10^{-3}$ ); they are spaced linearly in spin magnitudes and the cosine of the tilt angles. Results are given at a gravitational-wave frequency of 20 Hz.

Effectively all of the information comes from constraints on  $\chi_{\text{eff}}$  combined with the mass ratio (and our prior of isotropically distributed orientations and uniformly distributed magnitudes) [5].

The source's luminosity distance  $D_L$  is inferred from the signal amplitude [37,74]. The amplitude is inversely proportional to the distance, but also depends upon the binary's inclination [59,75–77]. This degeneracy is a significant source of uncertainty [57,71]. The inclination has a bimodal distribution with broad peaks for face-on and face-off orientations (see Fig. 4 of the Supplemental Material [11]). GW170104's source is at  $D_L = 880^{+450}_{-390}$  Mpc, corresponding to a cosmological redshift of  $z = 0.18^{+0.08}_{-0.07}$  [52]. While GW170104's source has masses and spins comparable to GW150914's, it is most probably at a greater distance [5,37].

For GW150914, extensive studies were made to verify the accuracy of the model waveforms for parameter estimation through comparisons with numerical-relativity waveforms [78,79]. GW170104 is a similar system to GW150914 and, therefore, it is unlikely that there are any significant biases in our results as a consequence of waveform modeling. The lower SNR of GW170104 makes additional effects not incorporated in the waveform models, such as higher modes [55,80,81], less important. However, if the source is edge on or strongly precessing, there could be significant biases in quantities including  $\mathcal{M}$  and  $\chi_{\text{eff}}$  [78]. Comparison to numerical-relativity simulations of binary black holes with nonprecessing spins [79], including those designed to replicate GW170104, produced results (and residuals) consistent with the model-waveform analysis.

## V. WAVEFORM RECONSTRUCTIONS

Consistency of GW170104 with binary black hole waveform models can also be explored through comparisons with a morphology-independent signal model [82]. We choose to describe the signal as a superposition of an arbitrary number of Morlet-Gabor wavelets, which models an elliptically polarized, coherent signal in the detector network. Figure 4 plots whitened detector data at the time of GW170104, together with waveforms drawn from the 90% credible region of the posterior distributions of the morphology-independent model and the binary black hole waveform models used to infer the source properties. The signal appears in the two detectors with slightly different amplitudes, and a relative phase shift of approximately  $180^\circ$ , because of their different spatial orientations [2]. The wavelet- and template-based reconstructions differ at early times because the wavelet basis requires high-amplitude, well-localized signal energy to justify the presence of additional wavelets, while the earlier portion of the signal is inherently included in the binary black hole waveform model.

The waveforms reconstructed from the morphology-independent model are consistent with the characteristic inspiral-merger-ringdown structure. The overlap [58]

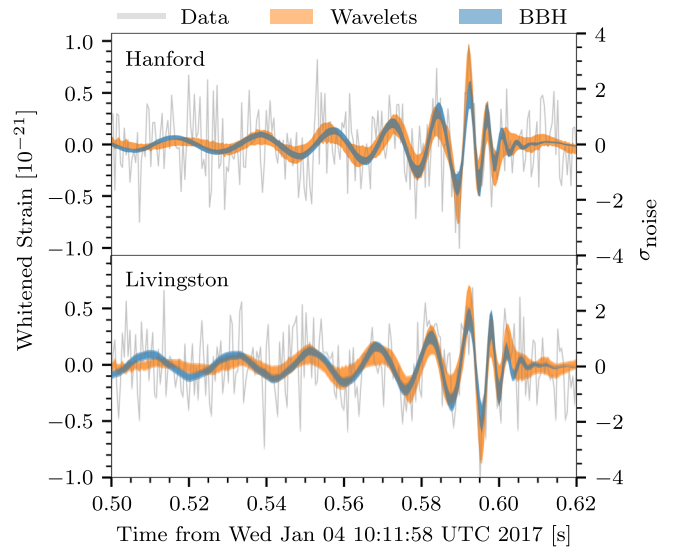


FIG. 4. Time-domain detector data (gray), and 90% confidence intervals for waveforms reconstructed from the morphology-independent wavelet analysis (orange) and binary black hole (BBH) models from both waveform families (blue), whitened by each instrument's noise amplitude spectral density. The left ordinate axes are normalized such that the amplitude of the whitened data and the physical strain are equal at 200 Hz. The right ordinate axes are in units of noise standard deviations. The width of the BBH region is dominated by the uncertainty in the astrophysical parameters.

between the maximum-likelihood waveform of the binary black hole model and the median waveform of the morphology-independent analysis is 87%, consistent with expectations from Monte Carlo analysis of binary black hole signals injected into detector data [34]. We also use the morphology-independent analysis to search for residual gravitational-wave energy after subtracting the maximum-likelihood binary black hole signal from the measured strain data. There is an 83% posterior probability in favor of Gaussian noise versus residual coherent gravitational-wave energy which is not described by the waveform model, implying that GW170104's source is a black hole binary.

## VI. BINARY BLACK HOLE POPULATIONS AND MERGER RATES

The addition of the first 11 days of coincident observing time in the second observing run, and the detection of GW170104, leads to an improved estimate of the rate density of binary black hole mergers. We adopt two simple representative astrophysical population models: a distribution that is a power law in  $m_1$  and uniform in  $m_2$ ,  $p(m_1, m_2) \propto m_1^{-\alpha}/(m_1 - 5M_\odot)$  with  $\alpha = 2.35$  [83], and a distribution uniform in the logarithm of each of the component masses [5,8]. In both cases, we impose  $m_1, m_2 \geq 5M_\odot$  and  $M \leq 100M_\odot$  [8]. Using the results from the first observing run as a prior, we obtain updated rates estimates of  $R = 103^{+110}_{-63} \text{ Gpc}^{-3} \text{ yr}^{-1}$  for the power

law, and  $R = 32^{+33}_{-20} \text{ Gpc}^{-3} \text{ yr}^{-1}$  for the uniform-in-log distribution [5]. These combine search results from the two offline matched filter analyses, and marginalize over the calibration uncertainty [32]. The range for the merger rate that brackets the two distributions,  $12\text{--}213 \text{ Gpc}^{-3} \text{ yr}^{-1}$ , is consistent with the range  $9\text{--}240 \text{ Gpc}^{-3} \text{ yr}^{-1}$  estimated from the first observing run [5,8]. Recalculating the rates directly after observing a new event can bias rate estimates, but this bias decreases with increasing event count and is negligible compared to other uncertainties on the intervals. While the median estimates have not changed appreciably, the overall tightening in the credible intervals is consistent with the additional observation time and the increment in the number of events with significant probability of being astrophysical from 3 to 4.

Following the first observing run, we performed a hierarchical analysis using the inferred masses of GW150914, LVT151012, and GW151226 to constrain the binary black hole mass distribution. We assumed the power-law population distribution described above, treating  $\alpha$  as a parameter to be estimated, and found  $\alpha = 2.5^{+1.5}_{-1.6}$  [5]. With the addition of GW170104,  $\alpha$  is estimated to be  $2.3^{+1.3}_{-1.4}$  (see Sec. IV of the Supplemental Material [11]); the median is close to the power-law exponent used to infer the (higher) merger rates.

## VII. ASTROPHYSICAL IMPLICATIONS

GW170104's source is a heavy stellar-mass binary black hole system. Such binaries are consistent with formation through several different evolutionary pathways [6]. Assuming black holes of stellar origin, there are two broad families of formation channels: dynamical and isolated binary evolution. Dynamical assembly of binaries is expected in dense stellar clusters [84–91]. Dynamical influences are also important for binary coalescences near galactic nuclei [92–94], and through interactions as part of a triple [95,96]. Isolated binary evolution in galactic fields classically proceeds via a common envelope [97–105]. Variants avoiding common-envelope evolution include (quasi-)chemically homogeneous evolution of massive tidally locked binaries [101,106,107], or through stable mass transfer in Population I [108,109] or Population III binaries [110,111].

Stars lose mass throughout their lives; to leave a heavy black hole as a remnant they must avoid significant mass loss. Low-metallicity progenitors are believed to have weaker stellar winds and hence diminished mass loss [112]. Given the mass of the primary black hole, the progenitors of GW170104 likely formed in a lower metallicity environment  $Z \lesssim 0.5Z_{\odot}$  [6,100,113–115], but low mass loss may also have been possible at higher metallicity if the stars were strongly magnetized [116].

An alternative to the stellar-evolution channels would be binaries of primordial black holes [117–120]. GW170104's

component masses lie in a range for which primordial black holes could contribute significantly to the dark matter content of the Universe, but merger rates in such scenarios are uncertain [118,121]. The potential for existing electromagnetic observations to exclude primordial black holes of these masses is an active area of research [119,122–128].

Some of the formation models listed above predict merger rates on the order of  $\sim 1\text{--}10 \text{ Gpc}^{-3} \text{ yr}^{-1}$  [85,87,92–96,107,110,115]. Given that the rate intervals have now tightened and the lower bound (from the uniform-in-log distribution) is  $\sim 12 \text{ Gpc}^{-3} \text{ yr}^{-1}$ , these channels may be insufficient to explain the full rate, but they could contribute to the total rate if there are multiple channels in operation. Future observations will improve the precision of the rate estimation, its redshift dependence, and our knowledge of the mass distribution, making it easier to constrain binary formation channels.

Gravitational-wave observations provide information about the component spins through measurements of  $\chi_{\text{eff}}$ , and these measurements can potentially be used to distinguish different formation channels. Dynamically assembled binaries (of both stellar and primordial black holes) should have an isotropic distribution of spin tilts, with equal probability for positive and negative  $\chi_{\text{eff}}$ , and a concentration around zero [129]. Isolated binary evolution typically predicts moderate ( $\lesssim 45^\circ$ ) spin misalignments [130], since the effect of many astrophysical processes, such as mass transfer [131,132] and tides [133,134], is to align spins with the orbital angular momentum. Black hole spins could become misaligned due to supernova explosions or torques during collapse. Large natal kicks are needed to produce negative  $\chi_{\text{eff}}$  by changing the orbital plane [129,130,135]. The magnitude of these kicks is currently uncertain [136–141] and also influences the merger rate, with high kicks producing lower merger rates in some population-synthesis models [98,100,115,142]. For binary neutron stars there is evidence that large tilts may be possible with small kicks [143–146], and it is not yet understood if similar torques could occur for black holes [138,147–149]. The absolute value of  $\chi_{\text{eff}}$  depends on the spin magnitudes. Small values of  $|\chi_{\text{eff}}|$  can arise because the spin magnitudes are low, or because they are misaligned with the orbital angular momentum or each other. The spin magnitudes for binary black holes are currently uncertain, but GW151226 demonstrated that they can be  $\gtrsim 0.2$  [3], and high-mass x-ray binary measurements indicate that the distribution of black hole spins could extend to larger magnitudes [147]. For GW170104, we infer  $\chi_{\text{eff}} = -0.12^{+0.21}_{-0.30}$ . This includes the possibility of negative  $\chi_{\text{eff}}$ , which would indicate spin-orbit misalignment of at least one component. It also excludes large positive values, and thus could argue against its source forming through chemically homogeneous evolution, since large aligned spins ( $a_i \gtrsim 0.4$ ) would be expected assuming the complete collapse of the progenitor stars [106]. The inferred range is consistent with dynamical assembly and isolated binary



evolution provided that the positive orbit-aligned spin is small (whether due to low spins or misalignment) [129,150–152]. Current gravitational-wave measurements cluster around  $\chi_{\text{eff}} \sim 0$  ( $|\chi_{\text{eff}}| < 0.35$  at the 90% credible level for all events; see Fig. 5 of the Supplemental Material [11]) [5]. Assuming that binary black hole spins are not typically small ( $\lesssim 0.2$ ), our observations hint towards the astrophysical population favoring a distribution of misaligned spins rather than near orbit-aligned spins [153]; further detections will test if this is the case, and enable us to distinguish different spin magnitude and orientation distributions [154–159].

### VIII. TESTS OF GENERAL RELATIVITY

To check the consistency of the observed signals with the predictions of GR for binary black holes in quasicircular orbit, we employ a phenomenological approach that probes how gravitational-wave generation or propagation could be modified in an alternative theory of gravity. Testing for these characteristic modifications in the waveform can quantify the degree to which departures from GR can be tolerated given the data. First, we consider the possibility of a modified gravitational-wave dispersion relation, and place bounds on the magnitude of potential deviations from GR. Second, we perform null tests to quantify generic deviations from GR: without assuming a specific alternative theory of gravity, we verify if the detected signal is compatible with GR. For these tests we use the three confident detections (GW150914, GW151226, and GW170104); we do not use the marginal event LVT151012, as its low SNR means that it contributes insignificantly to all the tests [5].

#### A. Modified dispersion

In GR, gravitational waves are nondispersive. We consider a modified dispersion relation of the form  $E^2 = p^2 c^2 + A p^\alpha c^\alpha$ ,  $\alpha \geq 0$ , that leads to dephasing of the waves relative to the phase evolution in GR. Here  $E$  and  $p$  are the energy and momentum of gravitational radiation, and  $A$  is the amplitude of the dispersion [160,161]. Modifications to the dispersion relation can arise in theories that include violations of local Lorentz invariance [162]. Lorentz invariance is a cornerstone of modern physics but its violation is expected in certain quantum gravity frameworks [162,163]. Several modified theories of gravity predict specific values of  $\alpha$ , including massive-graviton theories ( $\alpha = 0$ ,  $A > 0$ ) [163], multifractal spacetime [164] ( $\alpha = 2.5$ ), doubly special relativity [165] ( $\alpha = 3$ ), and Hořava-Lifshitz [166] and extra-dimensional [167] theories ( $\alpha = 4$ ). For our analysis, we assume that the only effect of these alternative theories is to modify the dispersion relation.

To leading order in  $AE^{\alpha-2}$ , the group velocity of gravitational waves is modified as  $v_g/c = 1 + (\alpha - 1)AE^{\alpha-2}/2$  [161]; both superluminal and subluminal propagation velocities are possible, depending on the sign of  $A$  and the value of  $\alpha$ . A change in the dispersion relation leads to an extra term

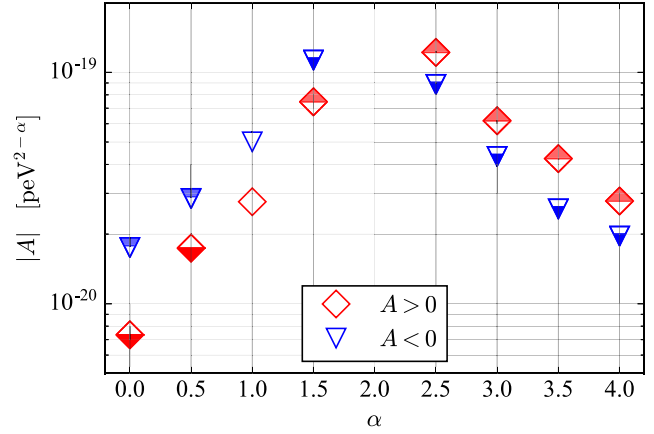


FIG. 5. 90% credible upper bounds on  $|A|$ , the magnitude of dispersion, obtained combining the posteriors of GW170104 with those of GW150914 and GW151226. We use picoelectronvolts as a convenient unit because the corresponding frequency scale is around where GW170104 has greatest amplitude ( $1 \text{ peV} \approx h \times 250 \text{ Hz}$ , where  $h$  is the Planck constant). General relativity corresponds to  $A = 0$ . Markers filled at the top (bottom) correspond to values of  $|A|$  and  $\alpha$  for which gravitational waves travel with superluminal (subluminal) speed.

$\delta\Psi(A, \alpha)$  in the evolution of the gravitational-wave phase [160]. We introduce such a term in the effective-precession waveform model [38] to constrain dispersion for various values of  $\alpha$ . To this end, we assume flat priors on  $A$ . In Fig. 5 we show 90% credible upper bounds on  $|A|$  derived from the three confident detections. We do not show results for  $\alpha = 2$  since in this case the modification of the gravitational-wave phase is degenerate with the arrival time of the signal.

There exist constraints on Lorentz invariance violating dispersion relations from other observational sectors (e.g., photon or neutrino observations) for certain values of  $\alpha$ , and our results are weaker by several orders of magnitude. However, there are frameworks in which Lorentz invariance is only broken in one sector [168,169], implying that each sector provides complementary information on potential modifications to GR. Our results are the first bounds derived from gravitational-wave observations, and the first tests of superluminal propagation in the gravitational sector.

The result for  $A > 0$  and  $\alpha = 0$  can be reparametrized to derive a lower bound on the graviton Compton wavelength  $\lambda_g$ , assuming that gravitons disperse in vacuum in the same way as massive particles [5,7,170]. In this case, no violation of Lorentz invariance is assumed. Using a flat prior for the graviton mass, we obtain  $\lambda_g > 1.5 \times 10^{13} \text{ km}$ , which improves on the bound of  $1.0 \times 10^{13} \text{ km}$  from previous gravitational-wave observations [5,7]. The combined bound using the three confident detections is  $\lambda_g > 1.6 \times 10^{13} \text{ km}$ , or for the graviton mass  $m_g \leq 7.7 \times 10^{-23} \text{ eV}/c^2$ .

#### B. Null tests

In the post-Newtonian approximation, the gravitational-wave phase in the Fourier domain is a series expansion in

powers of frequency, the expansion coefficients being functions of the source parameters [60,63,171]. In the effective-precession model, waveforms from numerical-relativity simulations are also modeled using an expansion of the phase in terms of the Fourier frequency. To verify if the detected signal is consistent with GR, we allow the expansion coefficients to deviate in turn from their nominal GR value and we obtain a posterior distribution for the difference between the measured and GR values [172–177]. We find no significant deviation from the predictions of GR [5,7]. Combined bounds for GW170104 and the two confident detections from the first observing run [5] do not significantly improve the bounds on the waveform phase coefficients.

Finally, we investigate whether the merger-ringdown portion of the detected signal is consistent with the inspiral part [7,178,179]. The two parts are divided at 143 Hz, a frequency close to the median inferred (detector-frame) innermost-stable-circular-orbit frequency of the remnant Kerr black hole. For each part, we infer the component masses and spins, and calculate from these the final mass and spin using fits from numerical relativity, as in Sec. IV [45–48]. We then calculate a two-dimensional posterior distribution for the fractional difference between final mass and spin calculated separately from the two parts [7,179]. The expected GR value (no difference in the final mass and spin estimates) lies close to the peak of the posterior distribution, well within the 90% credible region. When combined with the posteriors from GW150914, the width of the credible intervals decreases by a factor of  $\sim 1.5$ , providing a better constraint on potential deviations from GR.

In conclusion, in agreement with the predictions of GR, none of the tests we performed indicate a statistically significant departure from the coalescence of Kerr black holes in a quasicircular orbit.

## IX. CONCLUSIONS

Advanced LIGO began its second observing run on November 30, 2016, and on January 4, 2017 the LIGO-Hanford and LIGO-Livingston detectors registered a highly significant gravitational-wave signal GW170104 from the coalescence of two stellar-mass black holes. GW170104 joins two other high-significance events [2,3] and a marginal candidate [4] from Advanced LIGO’s first observing run [5]. This new detection is entirely consistent with the astrophysical rates inferred from the previous run. The source is a heavy binary black hole system, similar to that of GW150914. Spin configurations with both component spins aligned with the orbital angular momentum are disfavored (but not excluded); we do not significantly constrain the component black holes’ spin magnitudes. The observing run will continue until mid 2017. Expanding the catalog of binary black holes will provide further insight into their formation and evolution, and allow for tighter constraints on potential modifications to GR.

Further details of the analysis and the results are given in the Supplemental Material [11]. Data for this event are available at the LIGO Open Science Center [180].

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